



***Analysis of Dynamic Behaviors
of
Many TCP Connections
Sharing Tail-Drop / RED Routers***

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Backgrounds

- ***TCP (Transmission Control Algorithm)***
 - **Majority in the current Internet, also in the future**
- ***Analytic investigation is necessary to understand its characteristics***

Past researches on TCP throughput analysis

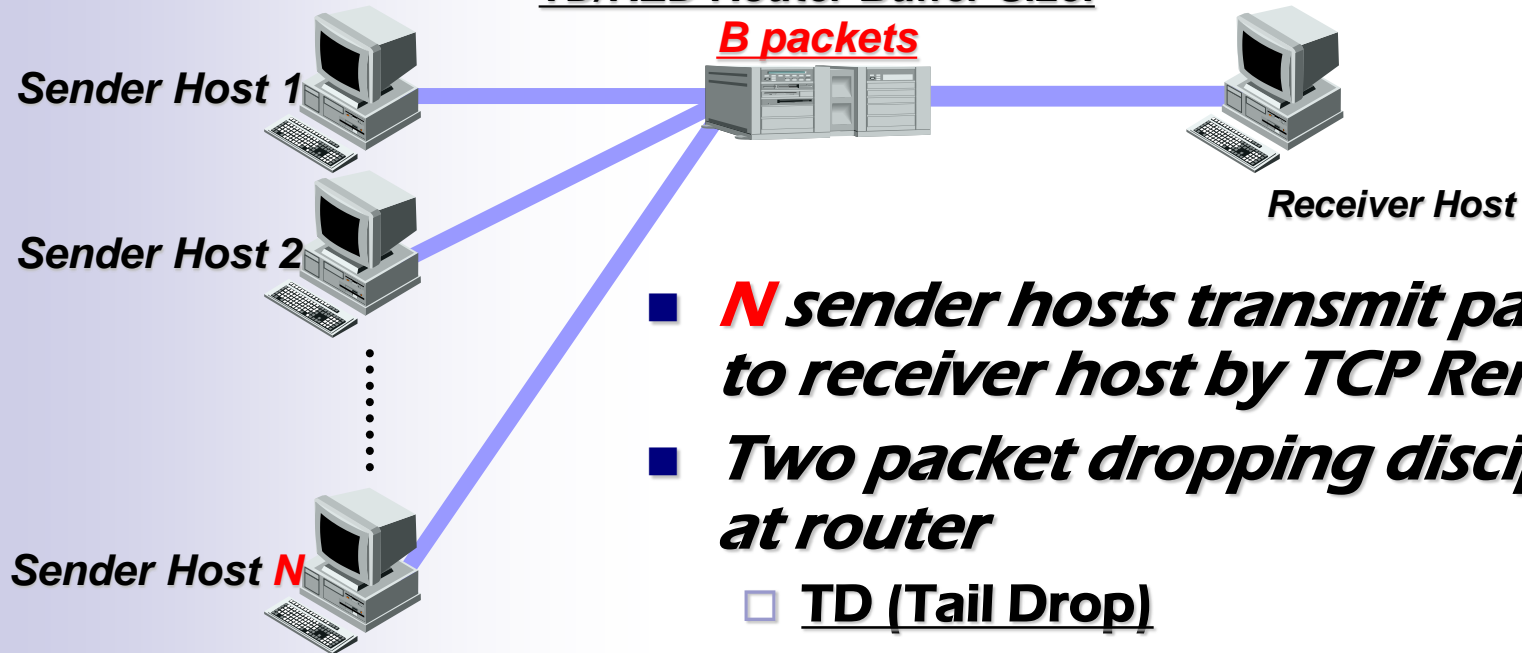
- **Long-term average throughput**
 - Short-term throughput is important for short file transfer
- **Assume constant packet loss ratio**
 - Packet loss ratio changes dynamically due to bursty packet loss
- **Assume RED works fine at the router**
 - Bad parameter setting degrades RED performance, causing bursty packet loss

Objectives

- *Analysis of **window size distribution** of TCP connections*
 - Using simple Markov modeling of TCP behavior
 - Many TCP connections accommodated
 - TD (Tail-Drop) and RED (Random Early Detection)
 - Effect of bursty packet loss
- *Evaluation of TD/RED routers in terms of ...*
 - Short-term fairness among TCP connections
 - Effect of poor parameter set of RED
 - Effect of TD buffer size

Network model

TD/RED Router Buffer Size:



- **N sender hosts transmit packets to receiver host by TCP Reno**
- **Two packet dropping disciplines at router**
 - TD (Tail Drop)
 - RED (Random Early Detection)
- **Focus on changes of window size, and ssthresh value of TCP connection**

Markov modeling of TCP behavior

- ***State is a **combination of window size and ssthresh** values of a TCP connection***
 - ***(w_i, t_i)***
- ***State transition occurs at every RTT***
 - ***cwnd increases when no packet loss occurs***
 - ***cwnd and ssth decrease when packet loss occurs***
- ***State transition probabilities are dependent on...***
 - ***Packet loss probability at the router buffer***
 - ***Slow start, congestion avoidance algorithms of TCP***

Increasing window size

- *When no packet loss occurs*
 - Probability: $(1 - p)^{w_i}$
- *State transition from (w_i, t_i) to ...*
 - $(2w_i, t_i)$
 - When $w_i < (1/2)t_i$ (Slow Start Phase)
 - (t_i, t_i)
 - When $(1/2)t_i < w_i < t_i$ (Phase Shift)
 - $(w_i + 1, t_i)$
 - When $t_i < w_i$ (Congestion Avoidance Phase)

Decreasing window size

- *When packet loss occurs*

- Probability: $1 - (1 - p)^{w_i}$

- *State transition from (w_i, t_i) to ...*

- $(1, w_i/2)$

- When timeout occurs

- $(w_i/2, w_i/2)$

- When fast retransmit occurs

- *Probability of timeout*

- Dependent on w_i and number of lost packets in a window

Packet loss probability: p

- *Past researches assume p is constant*
- *Actually dependent on...*
 - Router buffer size: **B**
 - Window size: **w_i**
 - Packet discarding discipline
 - TD (Tail Drop), RED (Random Early Detection)

Tail-drop router

- ***Bursty packet loss*** occurs when the router buffer overflows
- ***To calculate p , we have derived ...***
 - ***$P_{overflow}$*** : frequency of buffer overflow
 - ***$L_{overflow}$*** : # of lost packets in each buffer overflow
 - ***L_i*** : # of lost packets for each TCP connection in each buffer overflow
- ***$p = \min(1, P_{overflow} \cdot L_i / w_i)$***

Tail-drop router (2)

- ***P_{overflow}*** : *frequency of buffer overflow*
 - Considering queue dynamics
 - $1/(N(W_f - Nw')$
- ***L_{overflow}*** : *# of lost packets in each buffer overflow*
 - Each TCP connection increases its window size by 1 packet at every RTT
 - N packets are lost in total
- ***L_j*** : *# of lost packets for each TCP connection in each buffer overflow*
 - Proportional to window size of each TCP connection

RED router

- ***Packet discarding probability is determined from average queue length***
- ***For applying to our model, we use instantaneous queue length***

$$p_{red}(q) = \begin{cases} 0 & \text{if } q < min_{th} \\ \frac{q - max_{th}}{max_{th} - min_{th}} & \text{if } min_{th} \leq q < max_{th} \\ \frac{q \cdot max_p + (q - max_{th})}{q} & \text{if } max_{th} \leq q \end{cases}$$

RED router (2)

- ***q***: ***queue length***

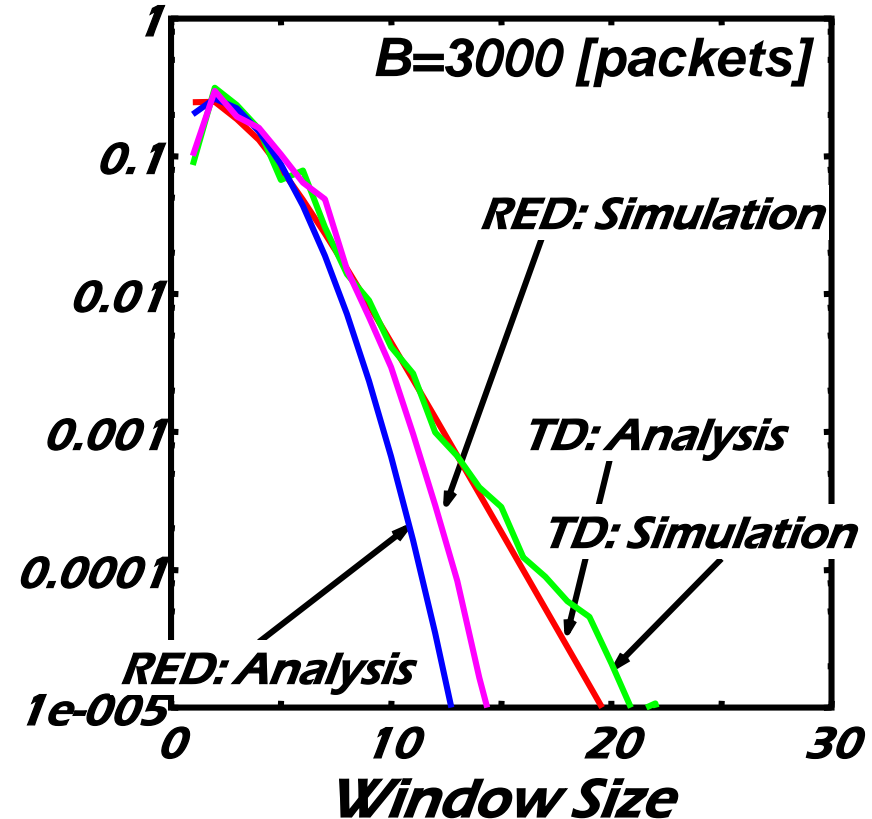
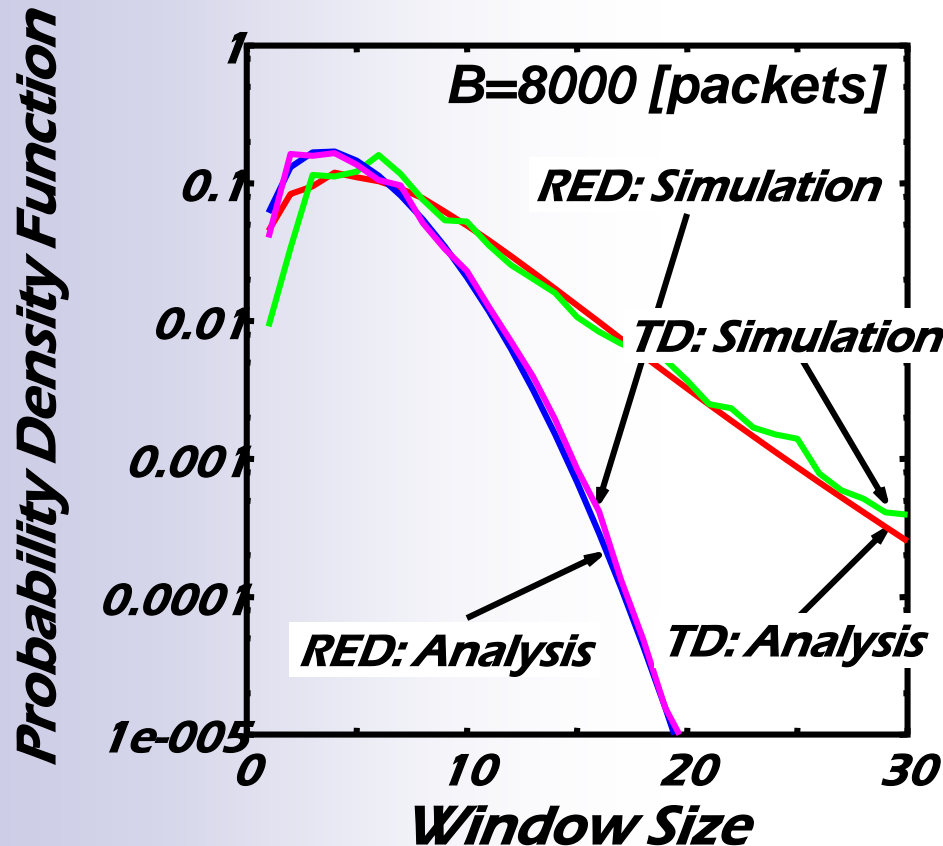
- Assume that other TCP connections are in steady state, and queue length is affected only by w_i

- $q = ((N-1)/N)w^* + w_i - 2\tau\rho$

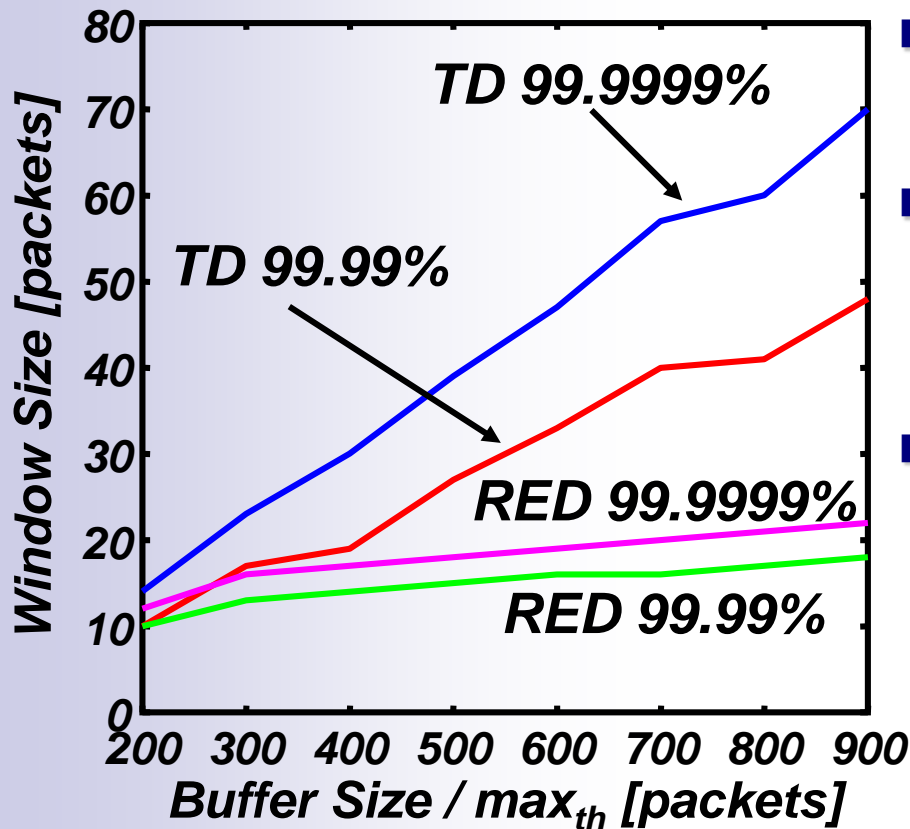
- $p = p_{red}(q)$

Accuracy of Analysis

- $N=1000$, $BW=1.5$ Mbps, $\tau = 2$ msec



Fairness evaluation



- ***Fairness of TD is much affected by buffer size***
- ***Variation of window size of RED is small, regardless of buffer size***
- ***RED can provide better fairness in short-term TCP throughput***

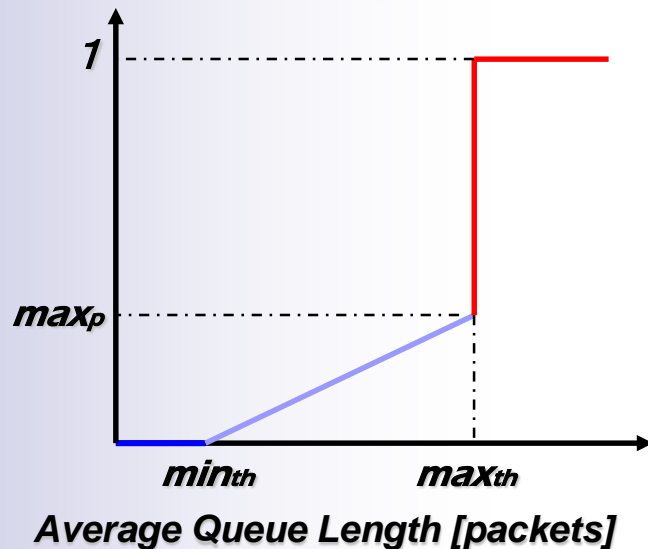
Conclusion

- ***Analysis of window size distribution of TCP connections***
 - **TD/RED disciplines**
 - **Burst packet loss**
- ***Fairness evaluation of TD/RED router***
 - **RED can give short-term fairness among connections**

RED router

- ***Probability is changed according to average queue length***
- ***Avoid buffer overflow, keep queue length low***

Packet Discarding Probability



Queue Length [packets]

