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On the Packet Delay Distribution in Power-law Networks

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Power-law in the Internet

- The degree distribution of the Internet topology follows a power-law
 - Power-law: Probability $P(k)$ that a node has k links is proportional to $k^{-\gamma}$
 - A lot of nodes are connected to a few nodes
 - A few "hub nodes" are connected to a large number of nodes

[1] A.-L. Barabási and R. Albert, "Emergence of scaling in random networks," Science, vol. 286, pp. 509-512, Oct. 1999.

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Relationship between topologies and performance

- Structures of topologies are defined not only by degree distribution, but also by other factors
- Difference in structure leads to difference in performance [12]

These topologies have the same degree distribution. However, they have different structures.

[12] L. Li, D. Alderson, W. Willinger, and J. Doyle, "A first-principles approach to understanding the Internet's router-level topology," in ACM SIGCOMM Computer Communication Review, vol. 34, pp. 3-14, Oct. 2004.

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Research purpose

- Difference in structure leads to difference in performance
 - The power-law degree distribution is not enough to discuss performance of networks
- We focus on the relationships between structure of topology and packet-level behavior
 - each of nodes has end-to-end flow control functionality
- Goal
 - Investigation of the optimal structure for efficient packet forwarding
 - Proposal of a new topology design method with this achievement

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Contributions of this work

- Traffic behavior in power-law topologies
 - Many researches are discussed in flow-level, but end-to-end flow control is not concerned
 - End-to-end flow control has large impacts to traffic behavior
 - Traffic behavior in BA topologies with end-to-end flow control is discussed, but structures of topologies are not concerned
- Reveals the relationships between structures of topologies and traffic behavior with end-to-end flow control

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Network model

- Stop-and-wait flow control: Source node stops to sending a packet till it receives ACK packet from destination
- Uniform link capacity: Each outgoing link transfers 1 packet per 1 time unit
- Shortest path routing: If multiple shortest paths are found, the next node is selected randomly
- Unlimited buffer: Each outgoing link has unlimited FIFO queuing buffer

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Network topologies

- 2 topologies having different structures
 - The number of nodes and links is the same
 - AT&T Topology... Measured router-level topology of AT&T
 - BA (AT&T) Topology... Generated by BA model [1]

Measured AT&T topology
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Waiting time distribution

- Waiting time is the time from when a packet is stored in a buffer to when a packet is delivered to next node
- These 2 waiting time distributions are similar, in spite of different structures
 - They exhibit long-tail characteristics

AT&T (250,000 Sessions) BA (250,000 Sessions)

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Betweenness centrality distribution

- Betweenness centrality is the number of node pairs that pass through a link
 - The number of packets that pass through the link is proportional to the betweenness centrality of the link
- Similar waiting time distributions are caused by betweenness centrality distributions

AT&T BA

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End-to-end packet delay distribution

- In spite of the similar waiting time distributions, packet delay distributions are much different
 - In the AT&T topology, packet delay distribution has long-tail
- Difference in structure leads to different packet delay distributions

AT&T BA

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Comparison the structures of the 2 topologies

- Why the delay distribution of the AT&T topology is long-tailed?
 - Comparing the structures of the 2 topologies
- Classification of the roles of the nodes [17]
 - Separating a topology into some modules
 - Participation coefficient, P [$0 \leq P \leq 1$]

Provincial Hubs Connector Hubs R7

R2 R3 R4

Participation coefficient, P

Within-module degree, W

R1: Ultra peripheral R5: Provincial hubs
R2: Peripheral R6: Connector hubs
R3: Non-hub connectors R7: Kinless hubs
R4: Kinless nonhub

The roles of the nodes categorized by this figure

$P_i = 0$ $P_j = 1$

Within-module degree, W

W_i is large, and W_j is small

[17] R. Guimerand, A. N. Amaral, "Functional cartography of complex metabolic networks," Nature, vol. 433, p. 895, 2005.

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The property of the structure of the BA topology

- The BA topology has many "Connector hubs"
 - Hub nodes have many links connecting to other modules
- Hub nodes transfer a large amount of packets between modules

Provincia Hubs Connector Hubs R7

R2 R3 R4

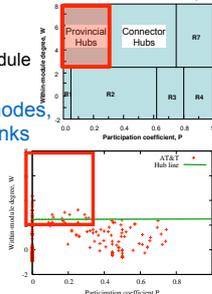
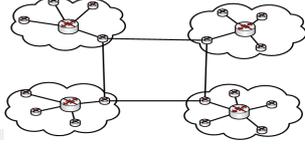
Participation coefficient, P

Within-module degree, W

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The property of the structure of the AT&T topology

- The AT&T topology has many “Provincial Hubs”
 - Hub nodes have many links connecting to the nodes in the same module
 - The AT&T topology has a few inter-module links
- First, packets are aggregated at hub nodes, and then forwarded via inter-module links



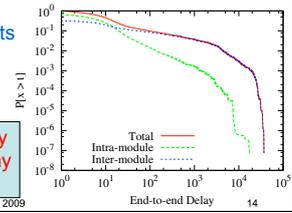
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Effects of structure of router-level topology

- Separating the packet delay distribution of the AT&T topology into intra-module packets and inter-module packets
 - The number of sessions is 250,000
 - Inter-module packets traverse through the inter-module links the rest is inter-module packets
- The packet delay distribution of inter-module packets exhibits a long-tail characteristic
 - Inter-module links in the AT&T topology tend to be congested



The structure of the AT&T topology lead to this long-tailed packet delay distribution

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Conclusions and future works

- Investigation of traffic behavior in power-law networks with end-host flow control (stop & wait protocol)
 - 2 topologies have different structures
 - 2 topologies have the similar waiting time distribution
- The structure of the AT&T topology makes the packet delay distribution long-tailed
 - “Connector hubs” and a few inter-module links
- Future works
 - Evaluations on topologies that have heterogeneous link capacity
 - Evaluations with more complex flow control like TCP
 - Evaluations of combination of flow control between routers and end-host flow control

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